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Fracture Height Growth in Layered Formations – Comprehensive Comparison of Modeled and Observed Data

Vibhas J. Pandey



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OUTLINE

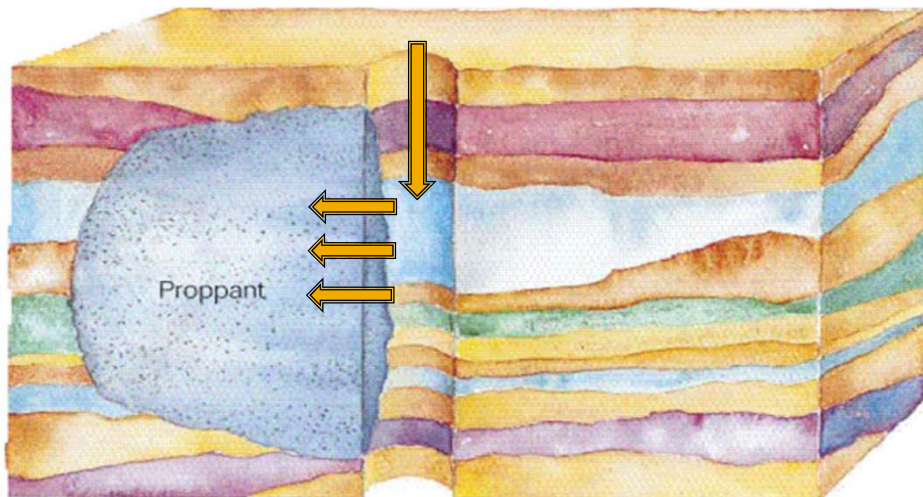


- Introduction
- Height growth in hydraulic fracturing treatment
- Fracture height prediction in layered models
- Development of fracture height growth model
- Comparison of modeled and field observations
- Modification of model for special cases
- Key parameters that influence fracture height growth
- Summary and Conclusions

Introduction



- Hydraulic fracturing: Popular well stimulation technique.
- Fluids are injected in downhole formations at pressures that exceed breakdown pressures, resulting in fractures that are then propped open to create a conductive pathway that eases the flow of hydrocarbons during the production phase.



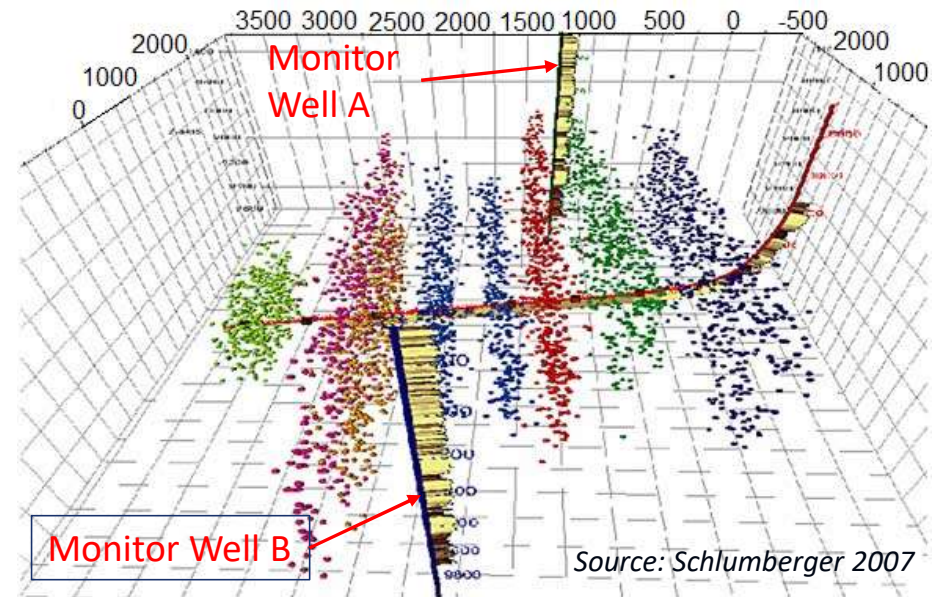
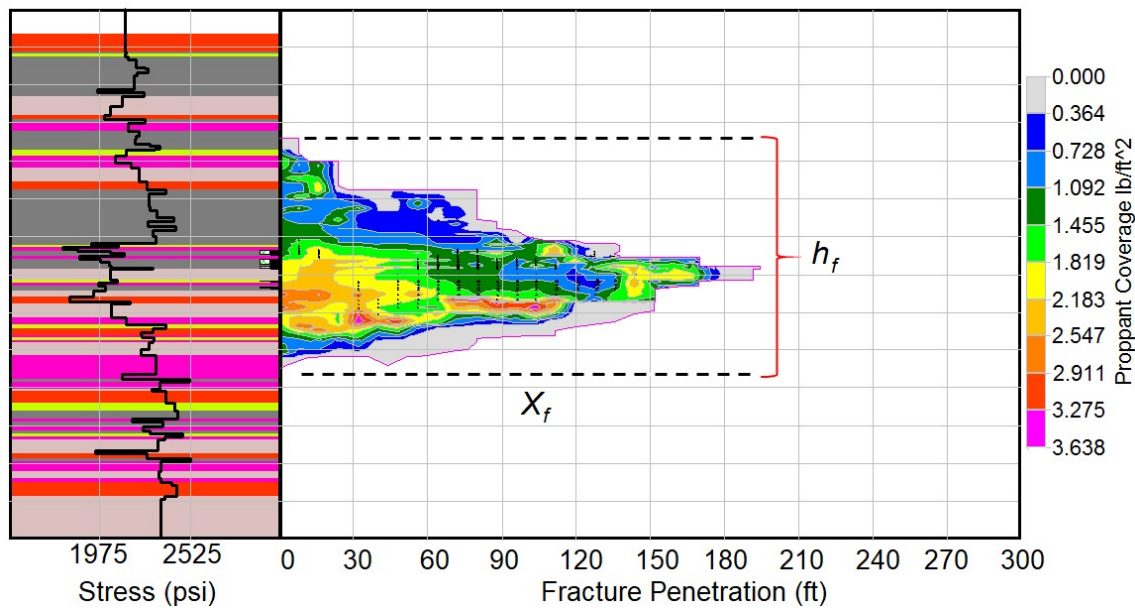
Source: Schlumberger Oilfield Reporter

- Key formation parameters
 - Stresses & Mechanical properties
 - Petrophysical Properties
- Controllable Parameters
 - Completion Method/Design
 - Injection rates and volumes
 - Fracturing Fluid properties

Typical Description of Fracture Geometry: X_f and h_f



- Fractures resulting from hydraulic fracturing treatments are generally described by their length (X_f) and height (h_f) dimensions.
- Planar features may be inferred from Microseismic survey data.



Fracture dimensions of half-length (X_f) and height (h_f) from fracture modeling simulators.

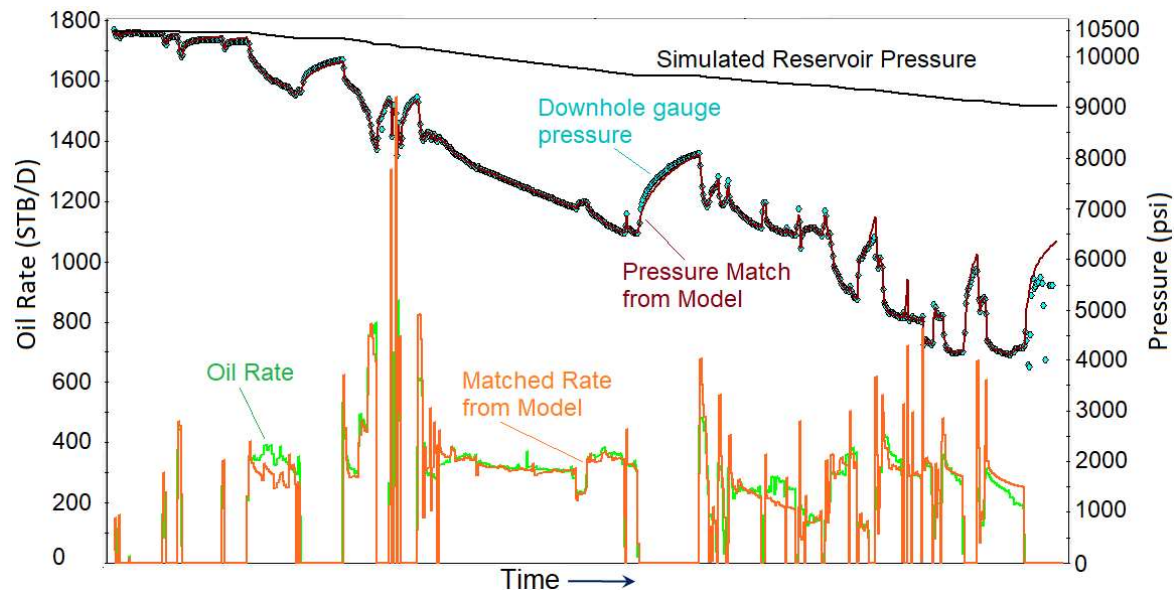
Microseismic (MS) survey data from an example well.

Why is h_f important in well stimulation?

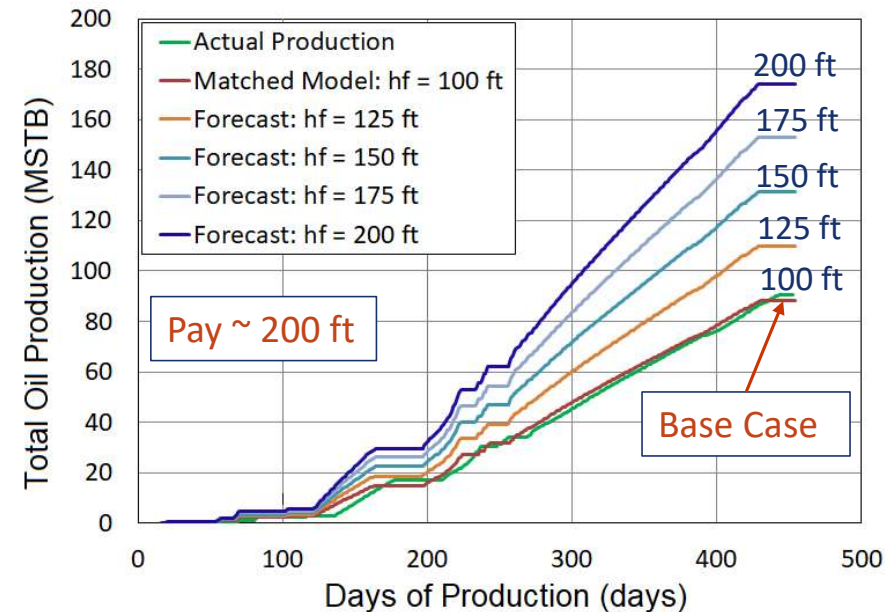


- Production rates are directly proportional to payzone height.
- Fracture dimensions contributing to production are obtained by history-match.

Production history match – horizontal well treatment.

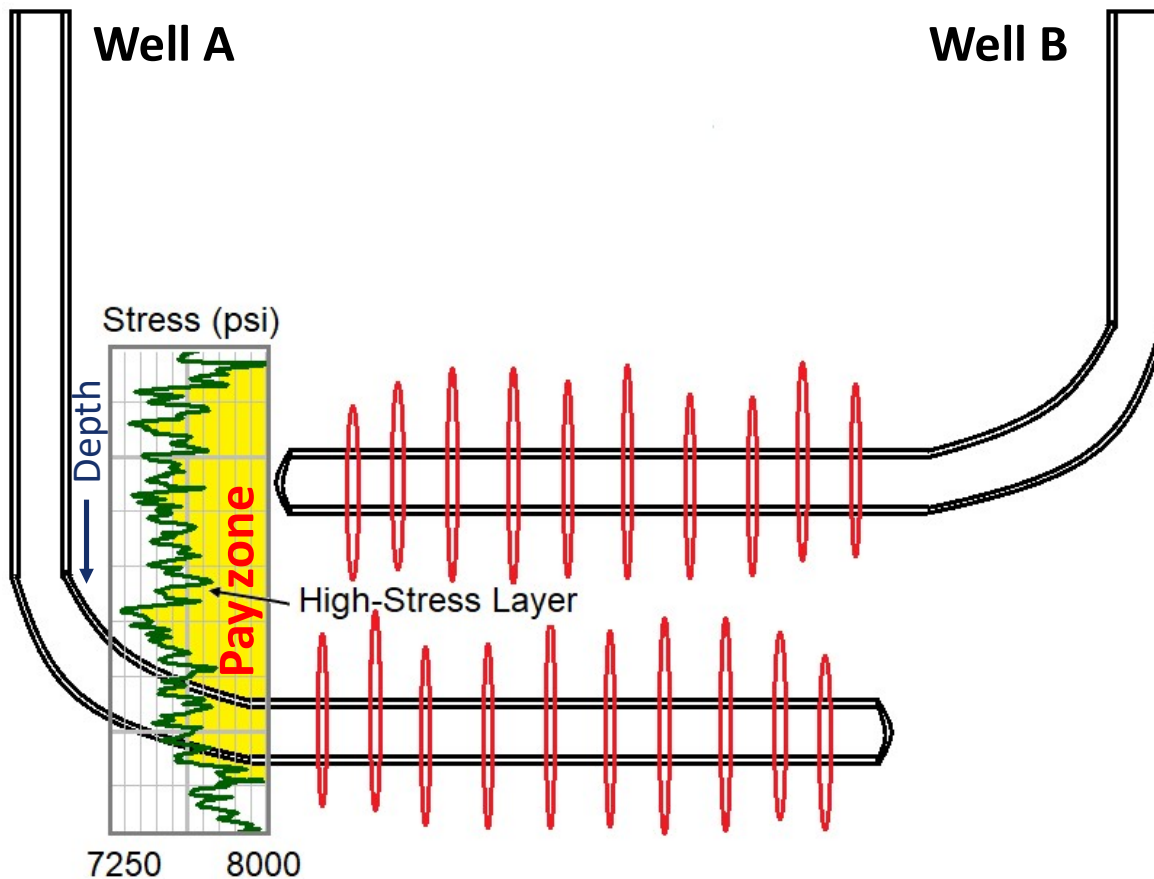


Production forecast - various fracture heights



Effective payzone coverage by propped fracture improves well performance.

Is desired fracture height always achievable?

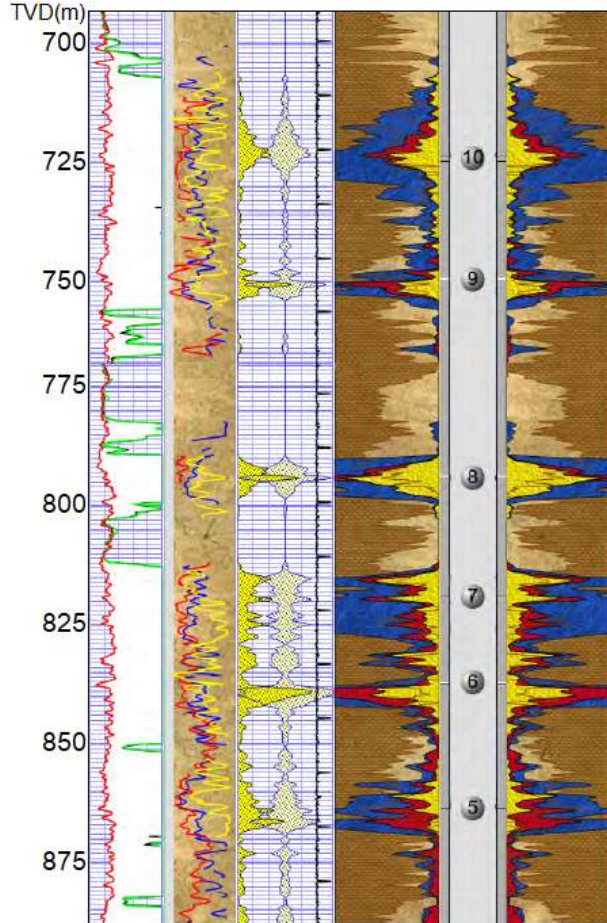


- High-stress layer(s) within the targeted zone can limit growth.
- Influence of geologic features.
- Expected fracture height during a treatment can influence:
 1. Well placement in horizontal well development program.
 2. Perforation depths and zoning in vertical wells.
 3. Treatment size and volume.

How tall do the hydraulic fractures grow anyway?

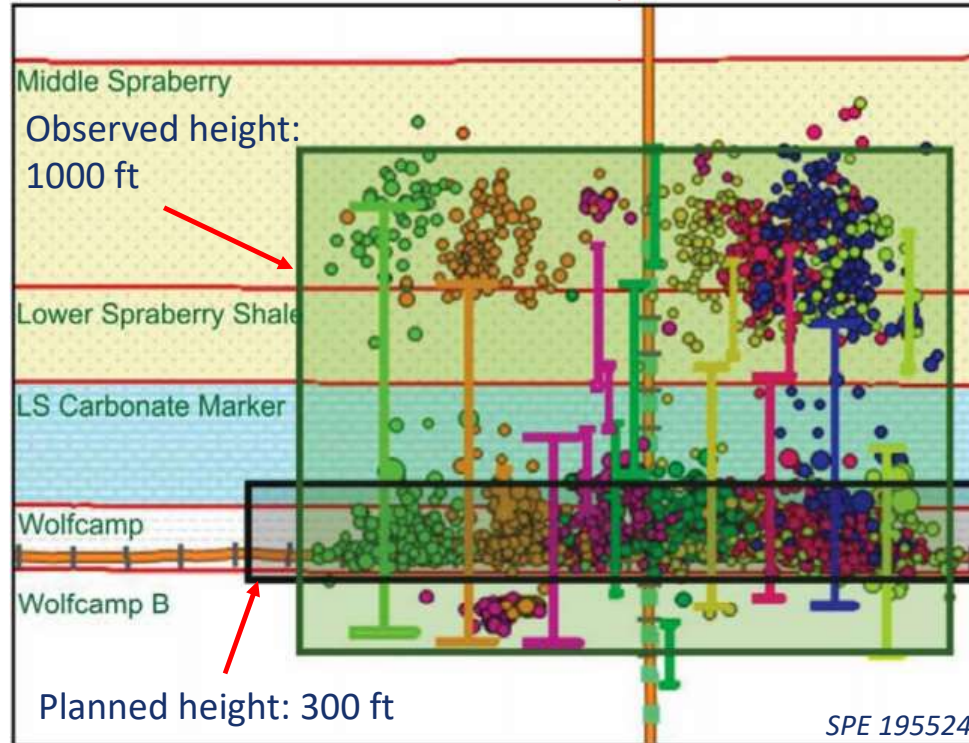


*RA Tracer: Vertical Well



- Growth is controlled by several factors.
- Field measurements show a wide range of h_f .

Microseismic and Tiltmeter Survey: Horizontal Well



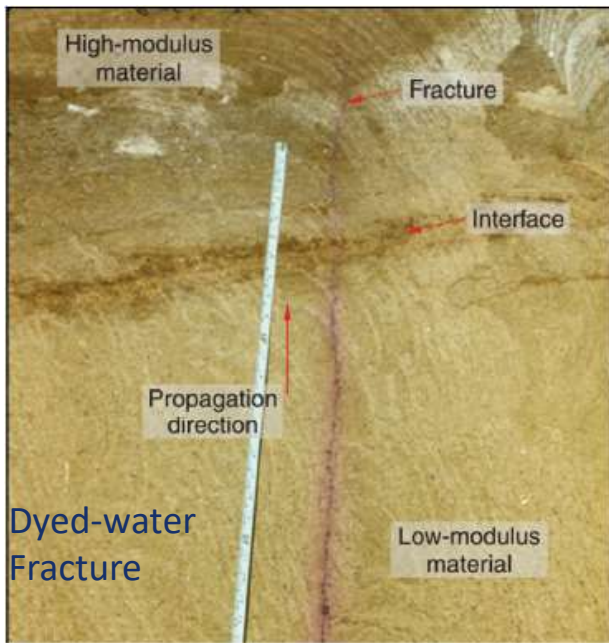
Observed fracture heights may significantly differ from planned heights.

*RA: Radioactive SPE 173378, SPE 176895

Does fracture growth terminate at interfaces?

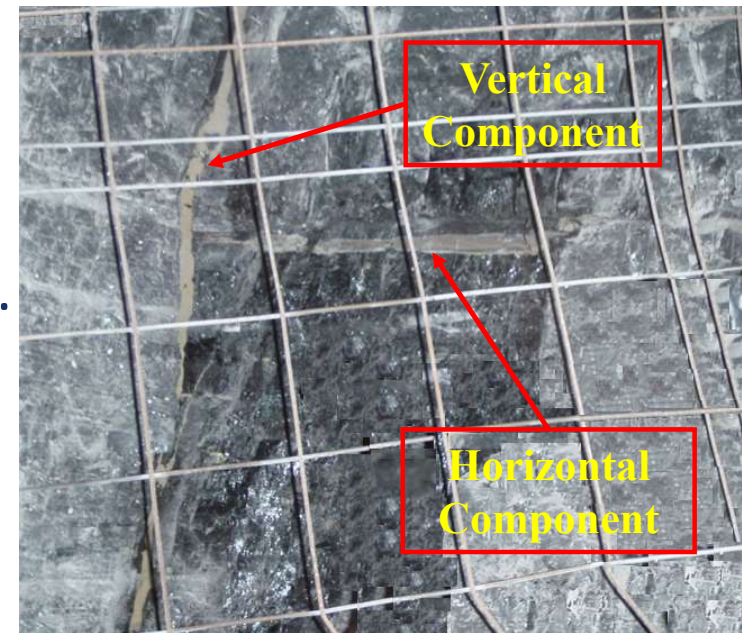


- Interfacial bonding – weak or strong may determine fracture crossing.
- Fractures may cross the layer interfaces and continue to propagate.
- Minebacks (shallow wells) suggest presence of horizontal fracture component.



SPE 145949

At shallower depths, horizontal fracture components may develop. Their contribution to production is generally minimal.



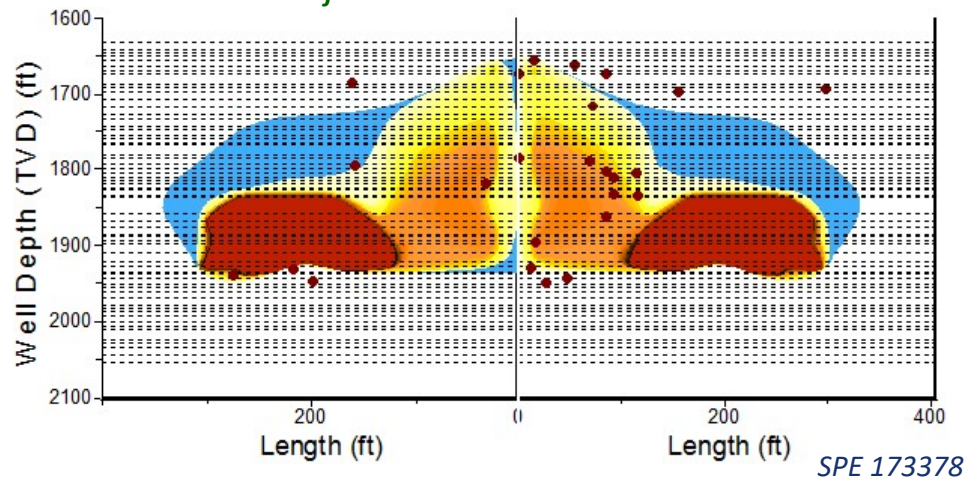
CBM Mineback 9

Do numerical simulators predict h_f accurately?

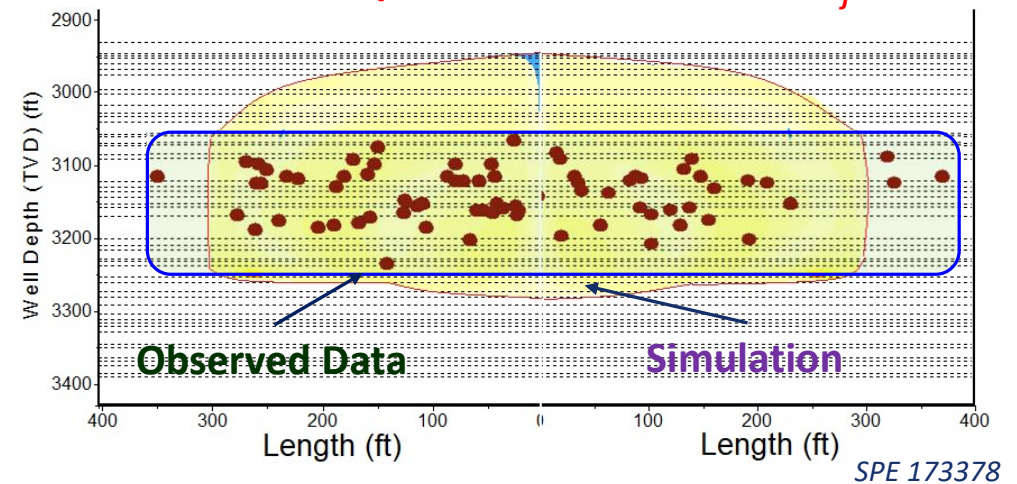


- Results vary – from reasonably good to incorrect predictions

Simulated h_f matches well with MS Events.



Mismatch of predicted and observed h_f .

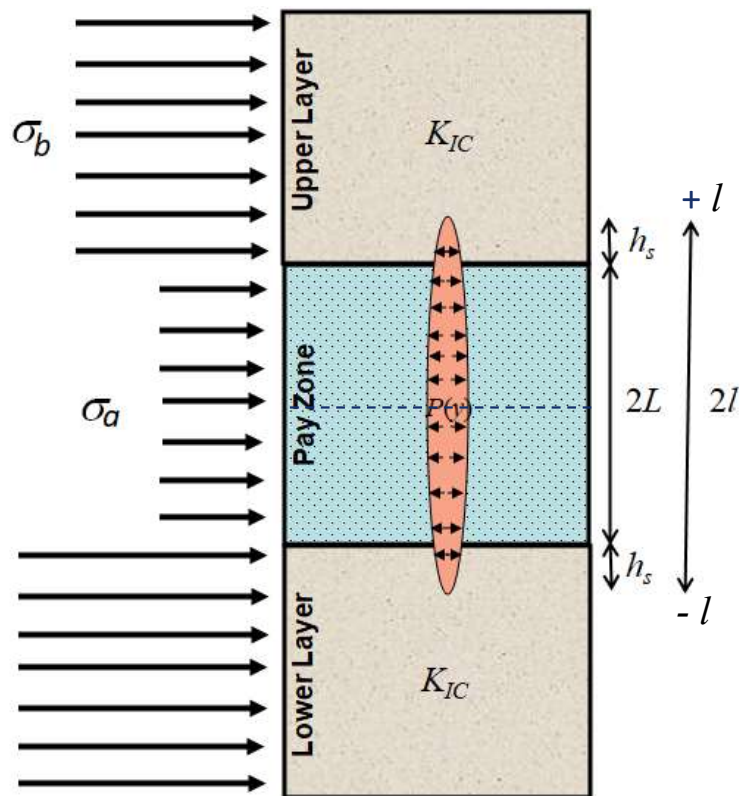


- Accurate prediction of fracture height growth is important
- Steps to improve fracture height predictions:
 1. Construct semi-analytical models and benchmark with literature data.
 2. Predict fracture height and calibrate with field data to improve the model.

Fracture Height Growth Estimation



- 3-Layered Solid Mechanics Model: Force-balance method



3-Layered Model – Asymmetric Stresses

$$K_I = \frac{1}{\sqrt{\pi l}} \int_{-l}^{+l} p(y) \sqrt{\frac{l+y}{l-y}} dy$$

$$K_I^{top,bot} = \frac{\sqrt{\pi l}}{2} (2p - \sigma_b - \sigma_c) \pm \frac{1}{\sqrt{\pi l}} (\sigma_c - \sigma_b) \sqrt{l^2 - L^2} + \sqrt{\frac{l}{\pi}} \sin^{-1} \left(\frac{L}{l} \right) (\sigma_c + \sigma_b - 2\sigma_a)$$

- h_s = fracture penetration, ft (m)
- K_I = stress Intensity factor, $\text{psi}\sqrt{\text{in}}$ ($\text{kPa}\sqrt{\text{m}}$)
- l = fracture half-height, ft (m)
- L = mid-layer thickness, ft (m)
- $p(y)$ = fracture pressure along crack-axis y , psi (MPa)
- σ = stresses in layers a, b & c, psi (MPa)

Net Pressure = Fracture Pressure – Closure Stress



Detour - Critical Stress Intensity Factor (K_{Ic})

- Fracture toughness (K_{Ic}) is material property but also geometry dependent.
- To account for possible changes as the fracture geometry evolves:
 - Fluid/tip velocity can be used to calculate K_{Ic}
 - Results can be directly incorporated in the Fracture Location vs. Net Pressure map.
- Governing equation (Pandey and Rasouli, 2021):

$$\Delta K_{Ic} = \left\{ v \left(\frac{\pi}{4} \right)^m \left(\frac{2n+1}{n} \right) \frac{1}{\phi(n)} \right\}^{\frac{n}{n+2}} \left[\frac{Kx^{2-\alpha}}{(1-\alpha)\cos[(1-\alpha)\pi]} \right]^{\frac{1}{n+2}} \left[\frac{E'\alpha}{2\sin(\alpha\pi)x^{\alpha-0.25}} \right]^{\frac{n+1}{n+2}}$$

E' = plane strain modulus, psi (MPa)

m = variable, function of power law index, n

n, K = Power Law indices

v = fluid (or fracture tip) velocity, ft/s (m/s)

x = distance from fracture tip, ft (m)

ΔK_{Ic} = apparent stress Intensity factor, $\text{psi}\sqrt{\text{in}}$ ($\text{kPa}\sqrt{\text{m}}$)

α = exponent (function of n), unitless

$\phi(n)$ = fluid flow equation variable

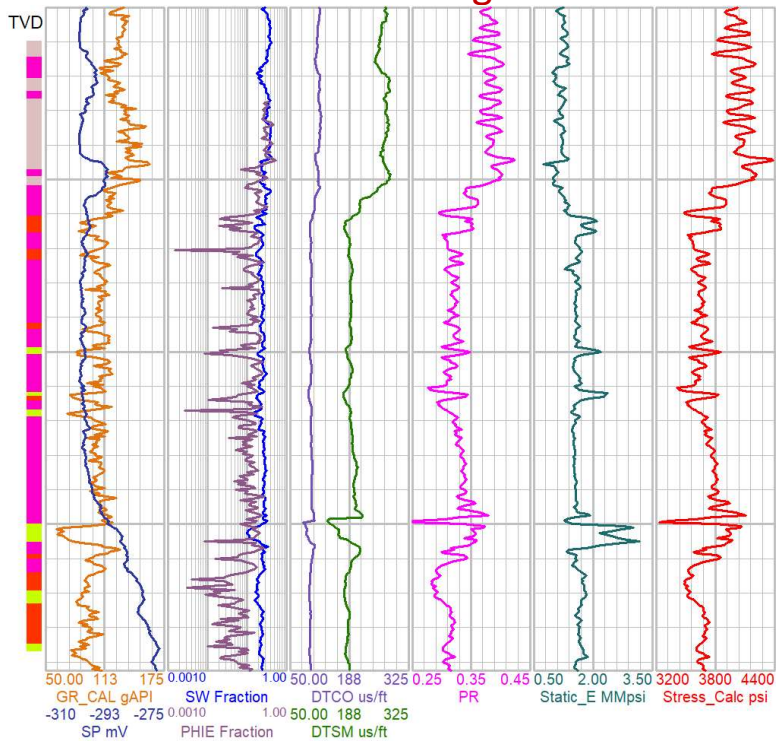
Fracture toughness may be calculated during simulations.

Real world cases are more complex

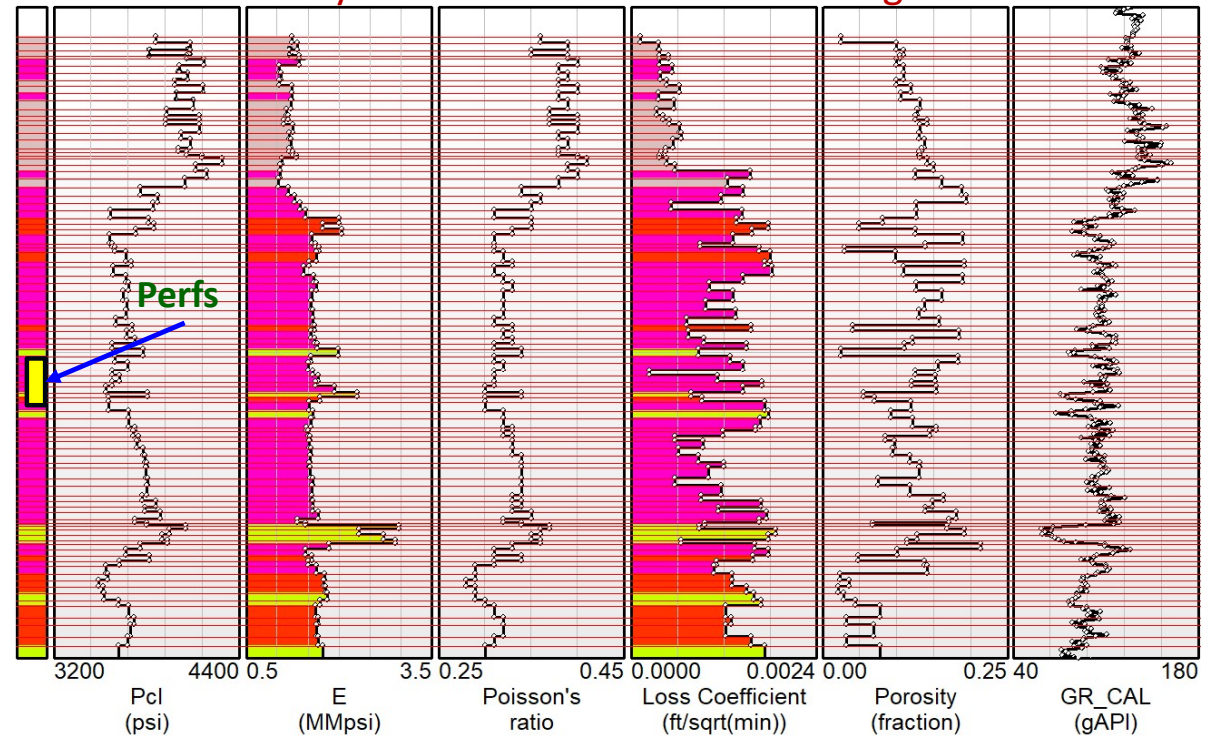


- Stress and mechanical property variations with depth are common.

Downhole Log Data



Layered Model Obtained from Log Data



Height growth models must account for variations in key formation properties.

Extending 3-Layer Solution to Multi-Layer Scenario



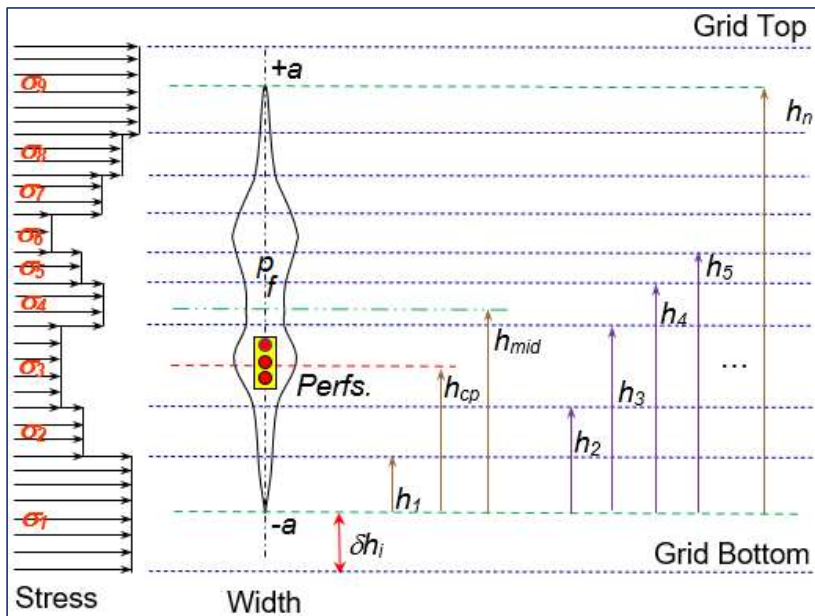
• Key Assumptions:

- Uniformly pressurized crack with no leak-off (*no fluid flow*)
- Fracture advances at slow-pace (*no tip effects*) in linearly elastic medium

$$K_I^{bot,top} = \sqrt{\frac{\pi h_f}{2}} \left[p_{cp} - \sigma_n + \rho_f g \left\{ h_{cp} - \frac{\xi h_f}{4} \right\} \right] + \sqrt{\frac{2}{\pi h_f}} \sum_{i=1}^{n-1} (\sigma_{i+1} - \sigma_i) \left[\frac{h_f}{2} \cos^{-1} \left(\frac{h_f - 2h_i}{h_f} \right) \pm \sqrt{h_i(h_f - h_i)} \right]$$

- g = gravitational acceleration, ft/s² (m/s²)
- h_{cp} = elevation to center of perforations, ft (m)
- h_i = elevation, ft (m)
- h_f = fracture height, ft (m)
- K_I = stress intensity factor, psi√in (kPa√m)
- p_{cp} = pressure at center of perforations, psi (MPa)
- ρ_f = fluid density, lbm/gal (kg/m³)
- ξ = tip location specific value (1 or 3)
- σ_n = stress at n^{th} layer, psi (MPa)

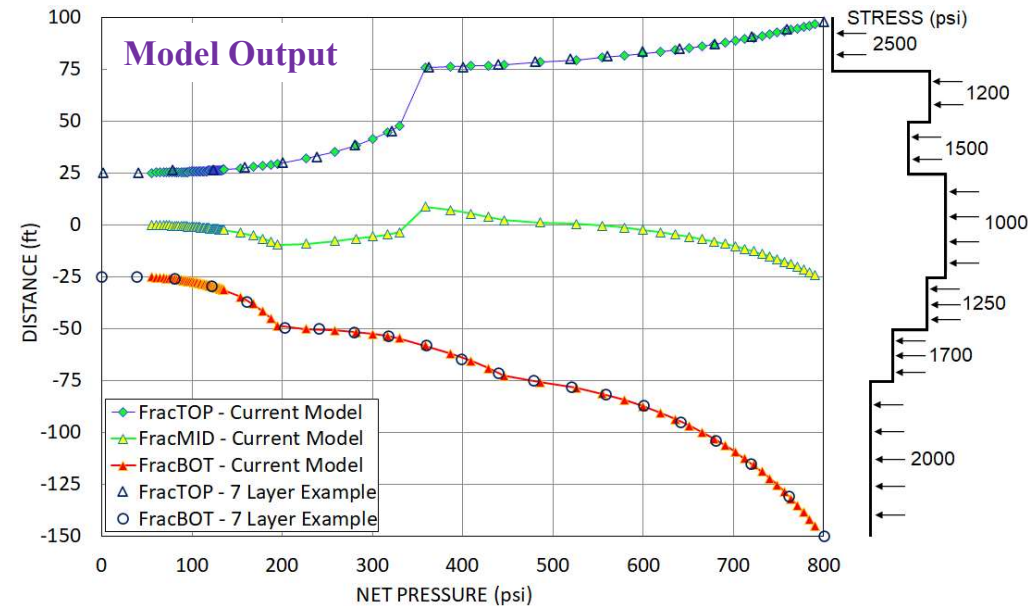
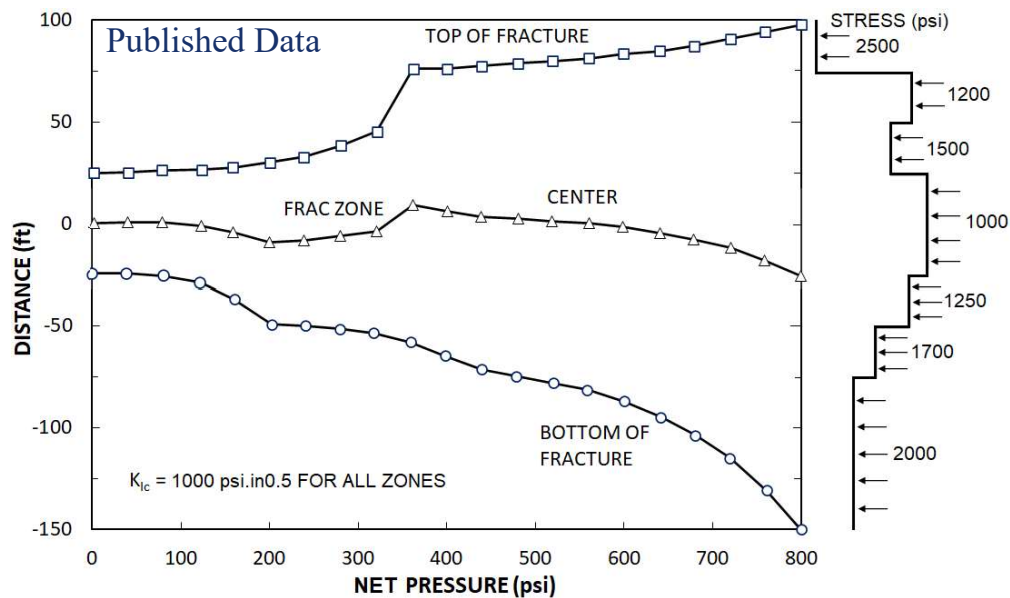
Solution is based on superposition of layered properties.



Constructing & Calibrating Height Growth Model



- Fracture height and location obtained by iteratively solving non-linear equations.
- Distance/Fracture Height vs. Net Pressure relation is generated as part of solution.

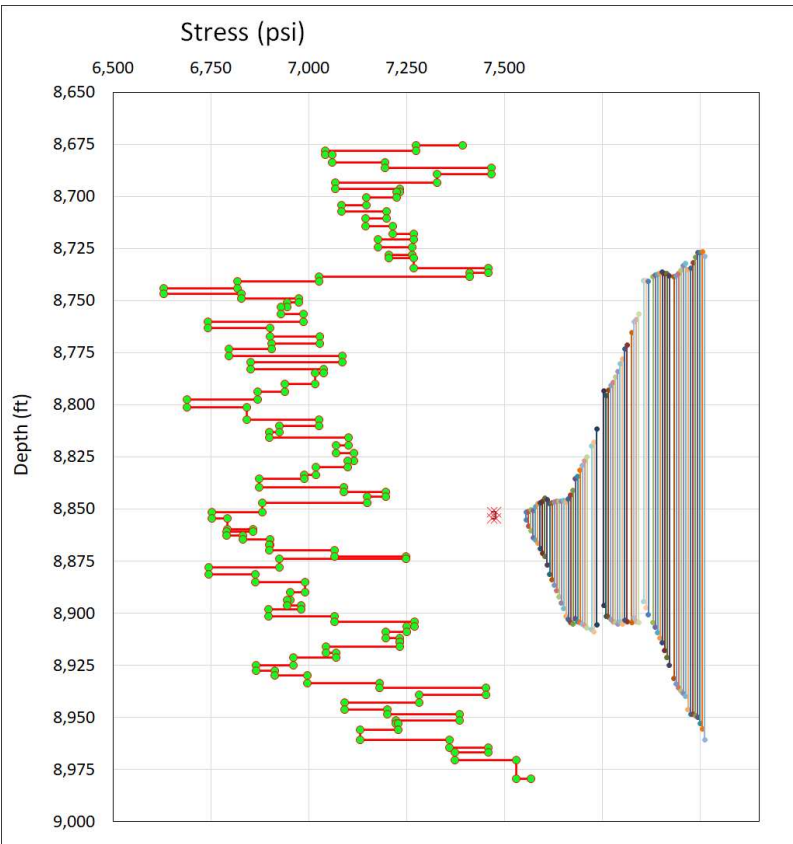


Fracture position and height are controlled by stress profile and fracture pressure.

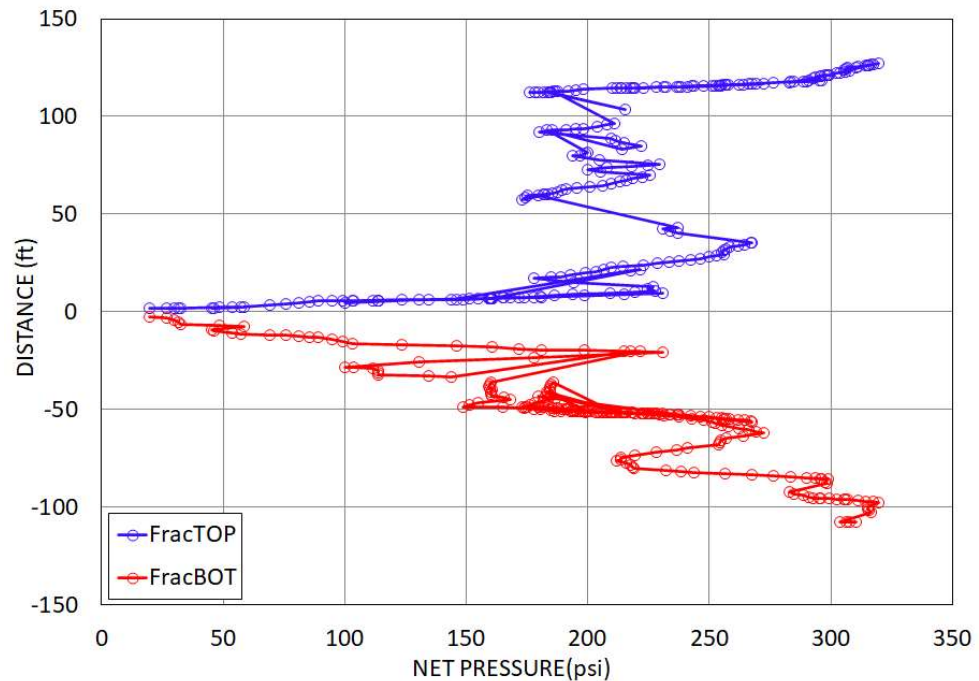
Model Application: Simulated Height Growth Evolution



- Vertical growth requires lower net pressure as high-stress layers are breached and low stress regions are exposed.
- Upward fracture growth is initially slow because of high stress layer at 8,240 ft but eventually fracture “migrates” upwards.



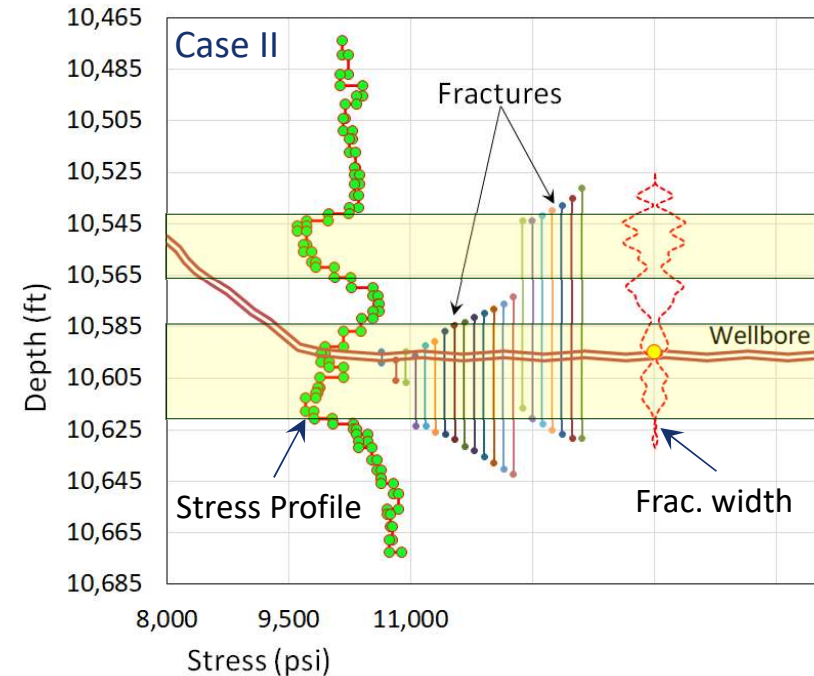
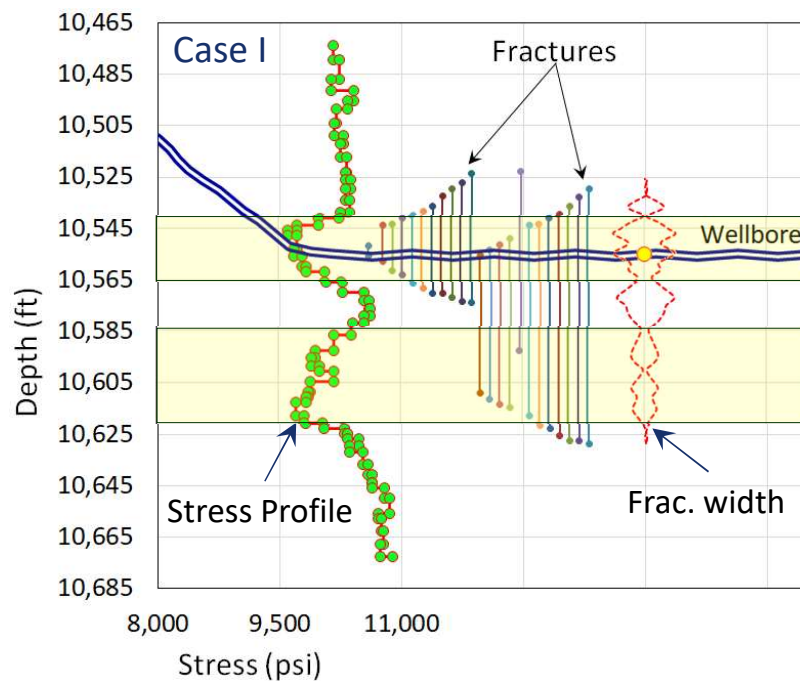
SPE-204155-MS



Model Application: Well Placement – Real Scenario



- Case I: Upward growth initially till the middle stress barrier at 10,575 ft is overcome.
- Case II: Initial fracture containment followed by upward growth.

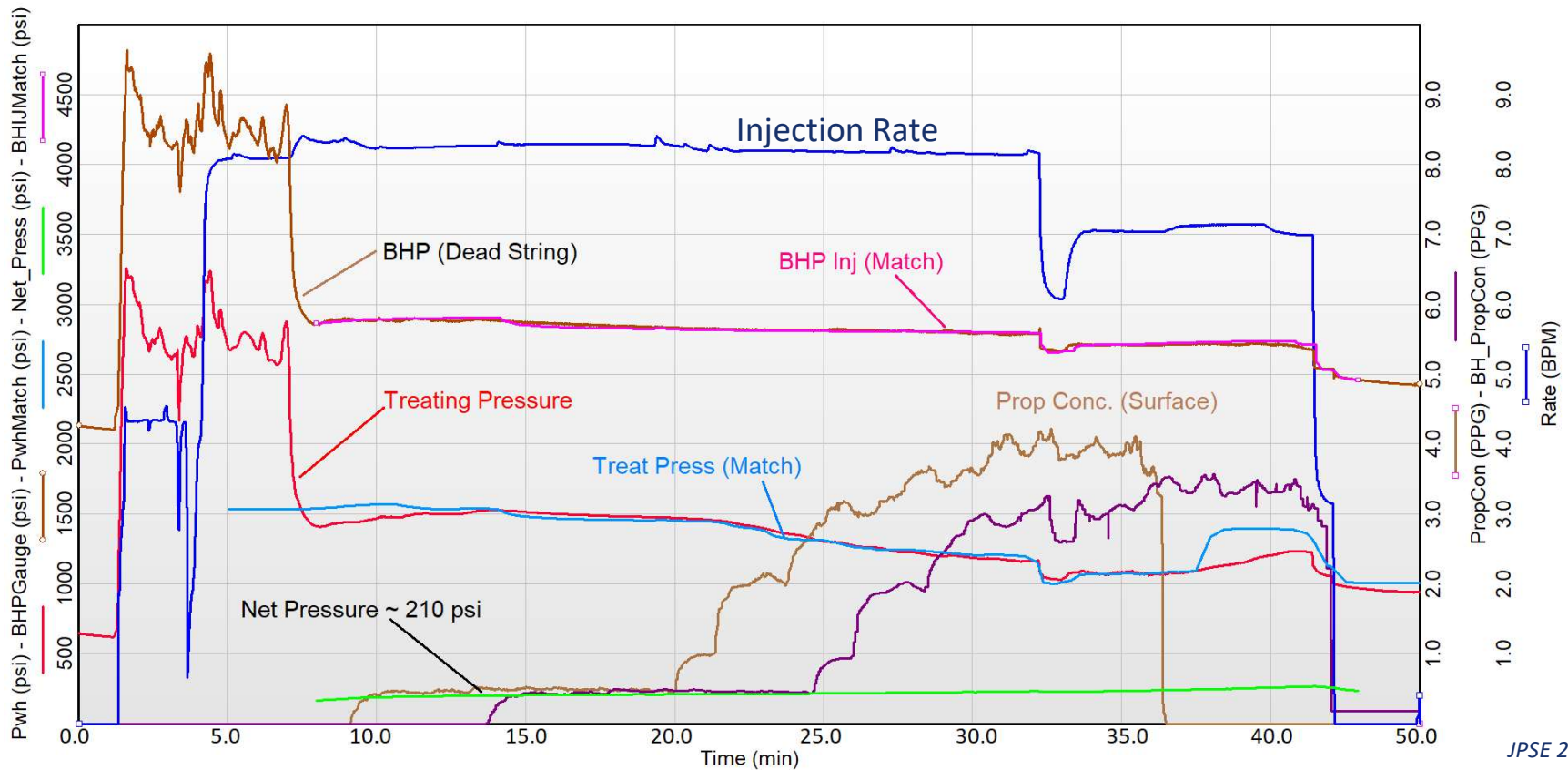


Height growth modeling can assist in optimal well placement.

Case History – I: Shallow Vertical CBM Wells



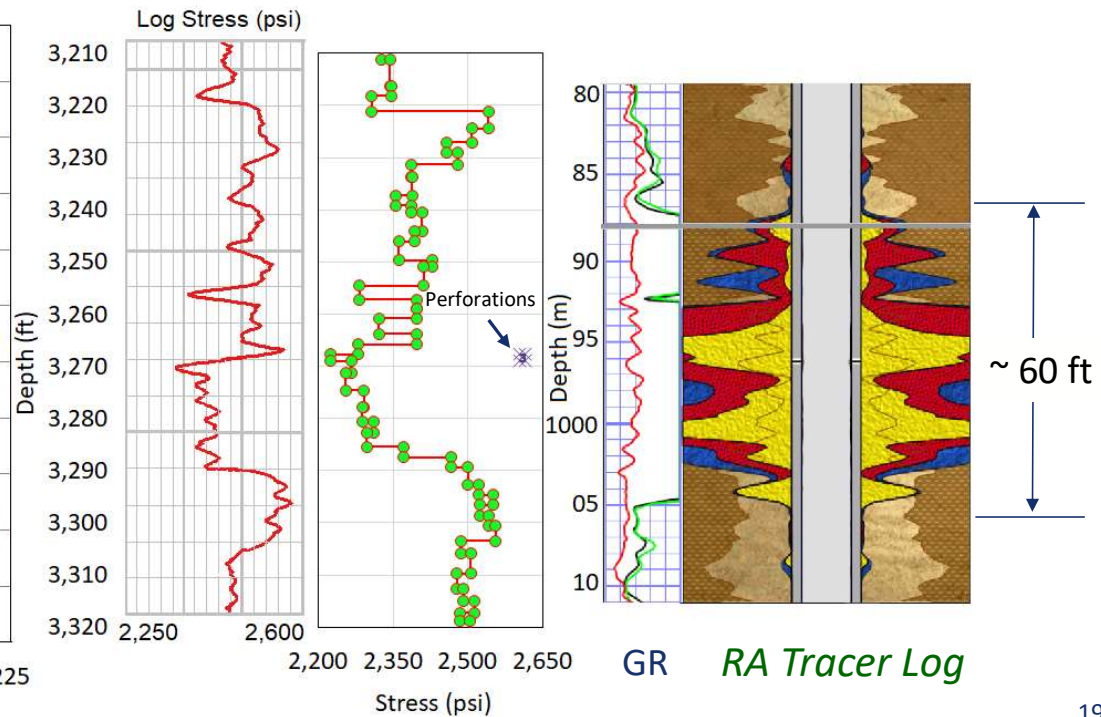
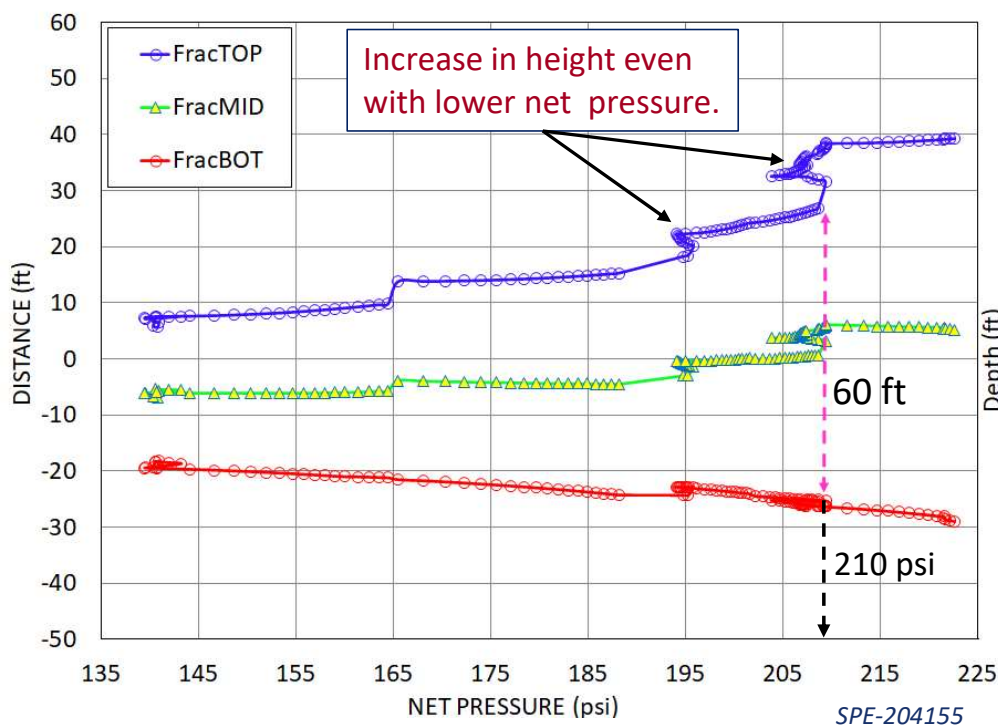
- 8.0 bbl/min; 1 7/8 C.T. × 4 1/2 in. Ann. , jet-cut holes, 20 lbm/Mgal x-linked fluid.



Case History – I: Shallow Vertical CBM Wells



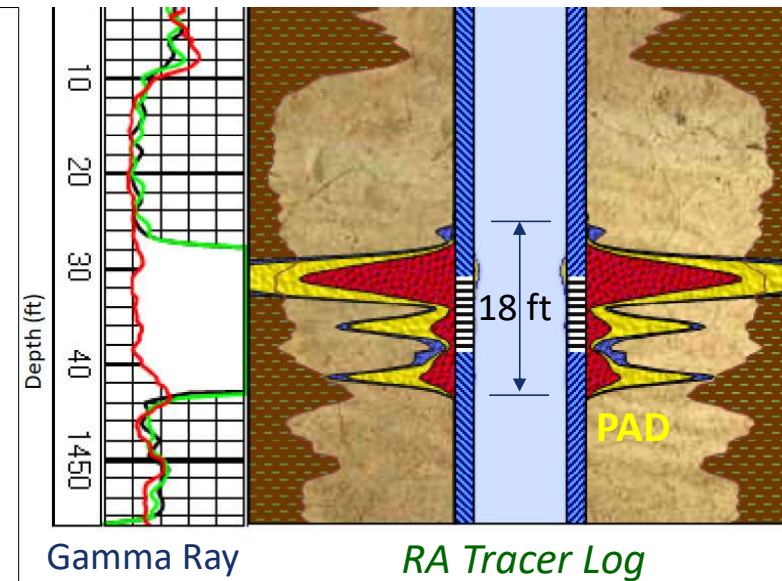
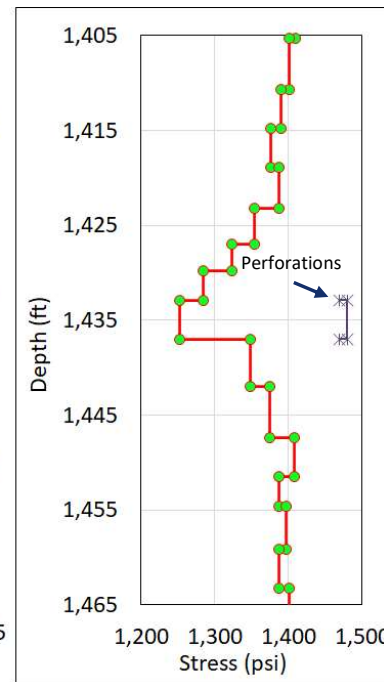
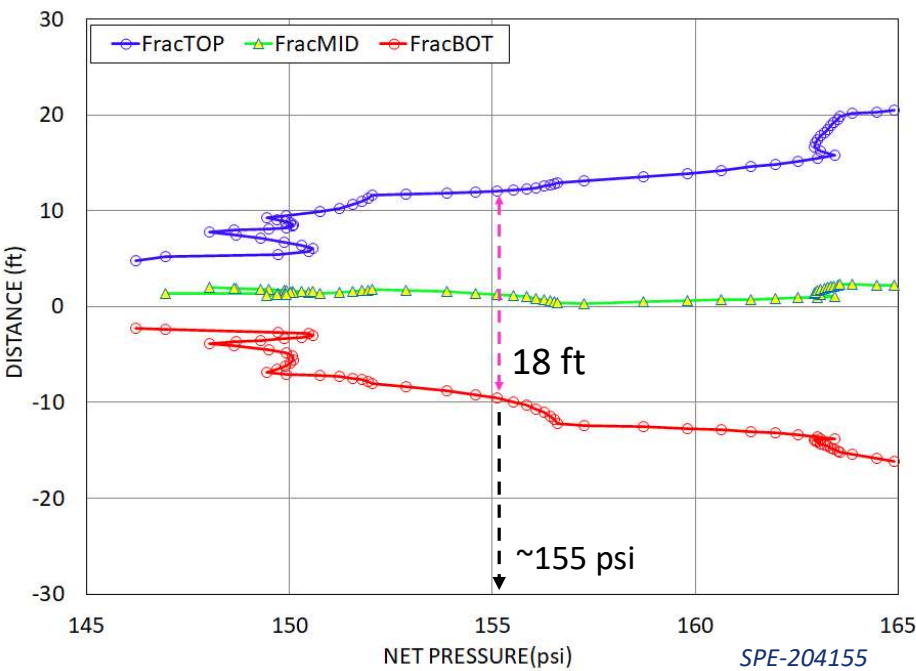
- 8.0 bbl/min down Ann. of 1 7/8 C.T. × 4 1/2 in. casing w/ 20 lbm/Mgal x-linked fluid.
- Predicted h_f and location matches the height derived from RA Tracer.



Case History – II: Shallow San Miguel Sands (S. TX)



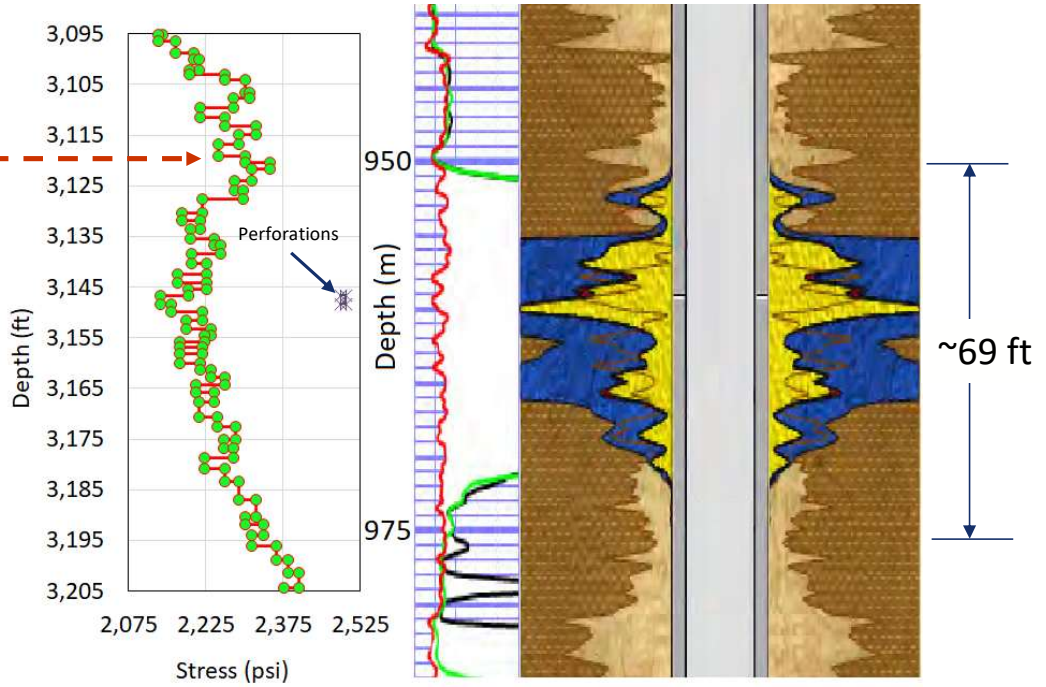
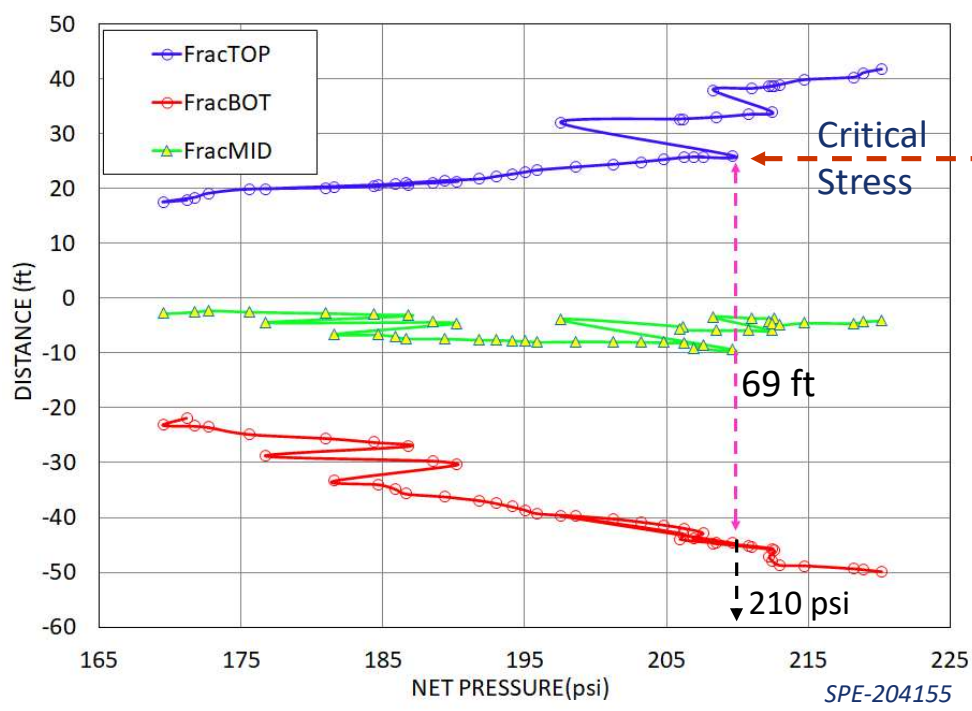
- 12 to 15 bbl/min down 4 ½ in. casing with 30 lbm/Mgal cross-linked fluid.
- BHP Injection exceeded overburden after 10 minutes of pumping.



Adjustments to Model : CBM Foam Frac Case History



- 8.0 bbl/min 65Q N₂ Foam with 20 lbm/Mgal cross-linked gel
- Model was modified to account for fluid flow induced fracture pressures.

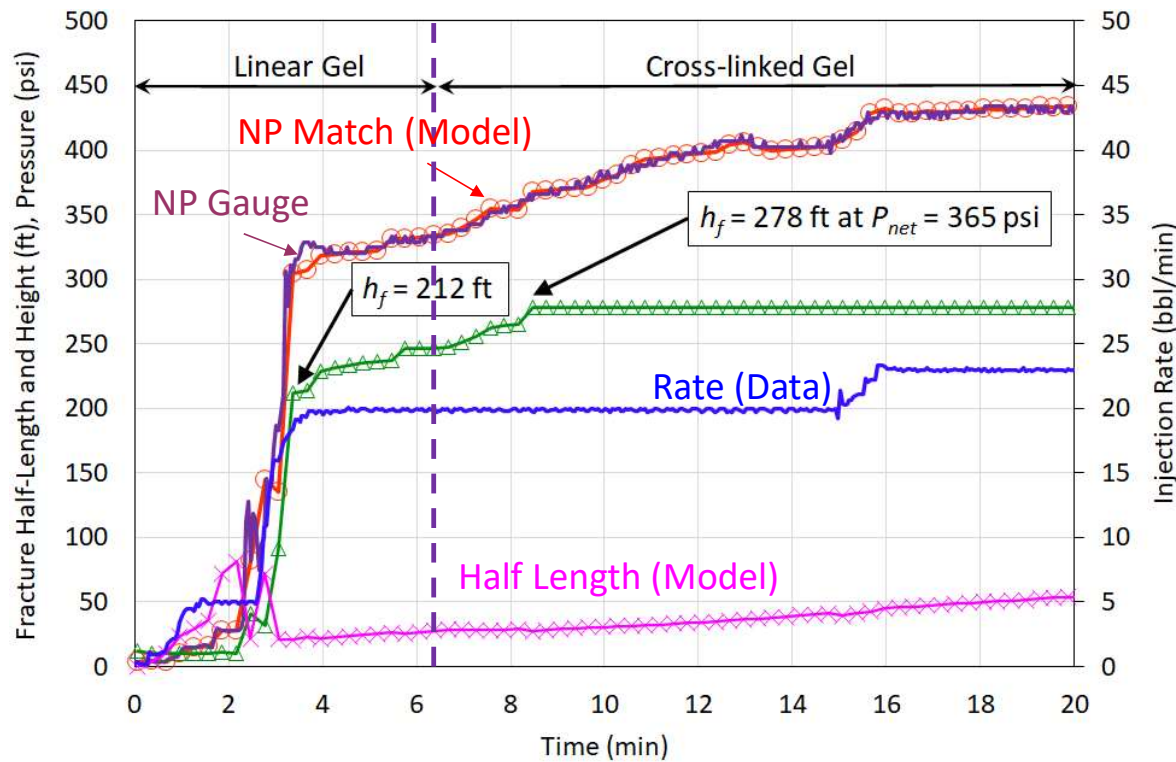


Superposition approach allows easy inclusion of other effects to base model.

Case History IV: Fracture Growth Rate (Sandstone)



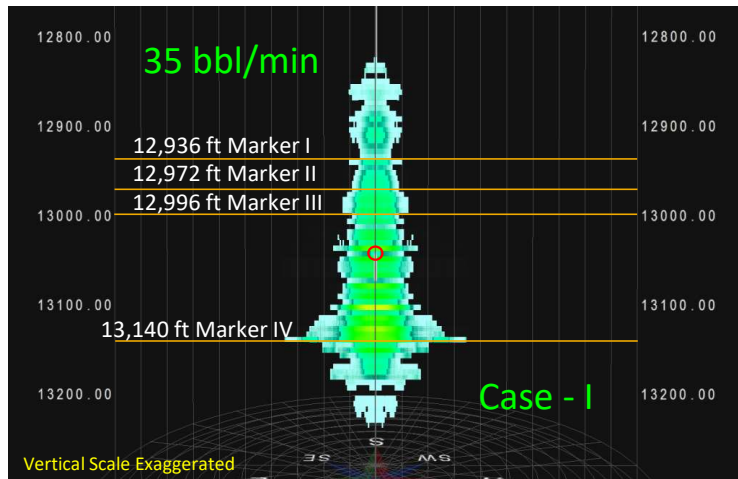
- Pressure History Match: 24.0 bbl/min with 30 lbm/Mgal x-linked gel



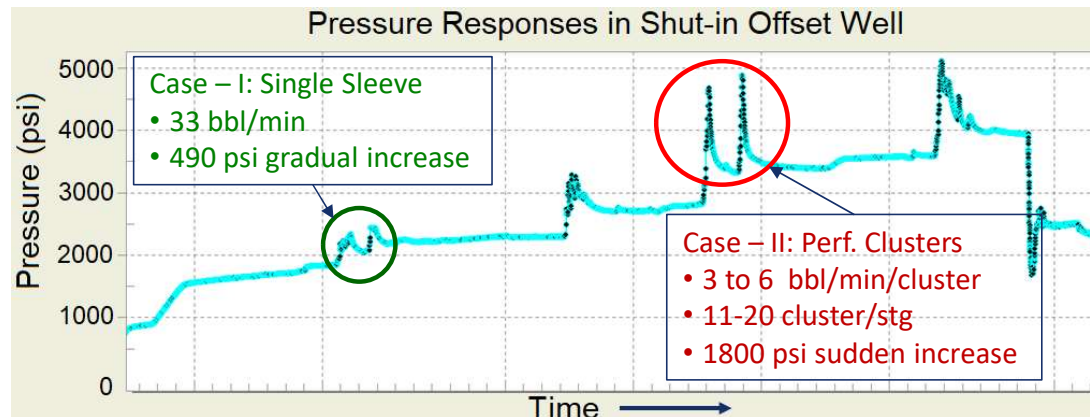
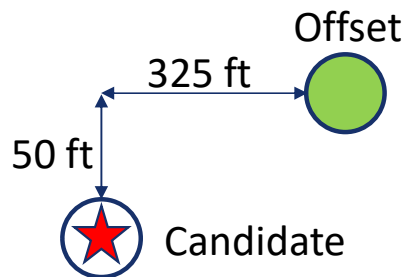
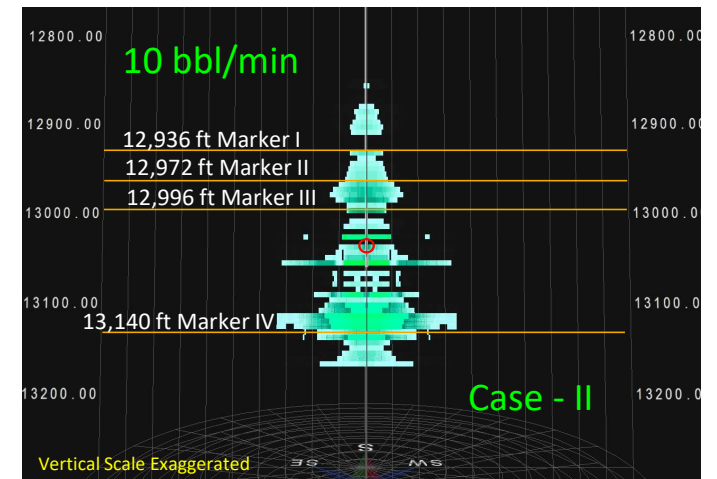
- Annulus Job: 1¾ in. x 4½ in.
- YM 3.0×10^6 psi (2.1×10^4 MPa)
- Poisson's Ratio ~ 0.25
- F.G. ~ 0.71 psi/ft (16.2 kPa/m).
- Leakoff 0.000168 ft/ $\sqrt{\text{min}}$ (0.0004 m/ $\sqrt{\text{s}}$)

Rapid increase of injection rate can accelerate fracture height growth.

Corroboration of Model Predictions with Field Data



- Rapid h_f growth from higher injection rates appears to limit X_f as predicted.

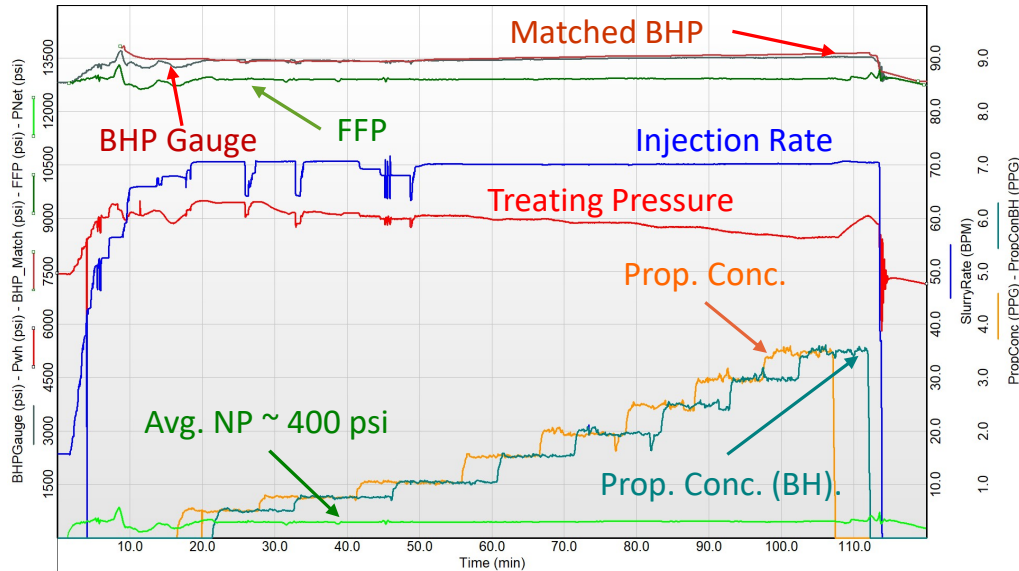


To wrap it up – Horizontal Well Case History

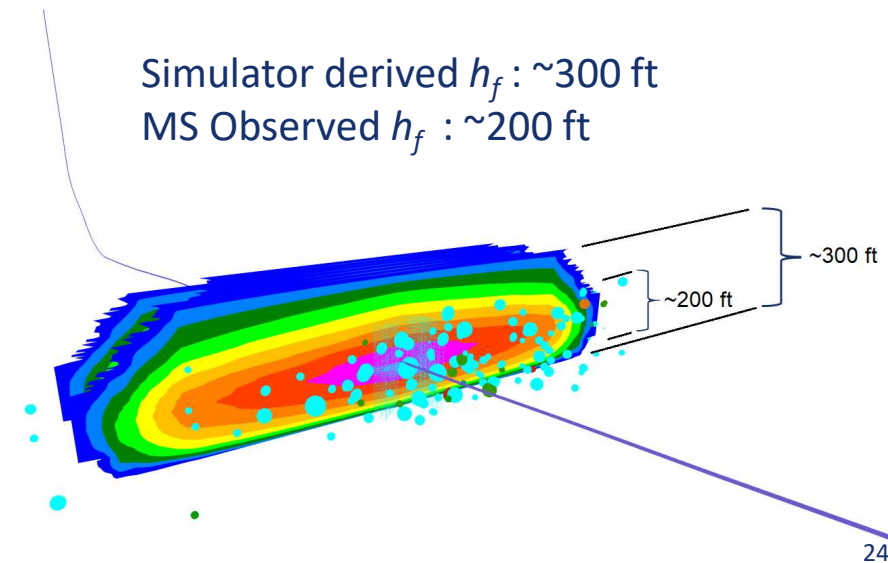


- Case History #5: 30 lbm/Mgal x-link, Shale Completion
 - Treatment pumped down 5½ in. casing at 70 bbl/min, 8 Perf Clusters, with Plug and Perf.
 - Formation Face Pressure - FFP (SPE 194351) *exceeds* the overburden during the job.
 - BHP and Microseismic measurements (survey) were carried out during the treatment.

History match of treatment data with simulator



Simulator derived height > observed height

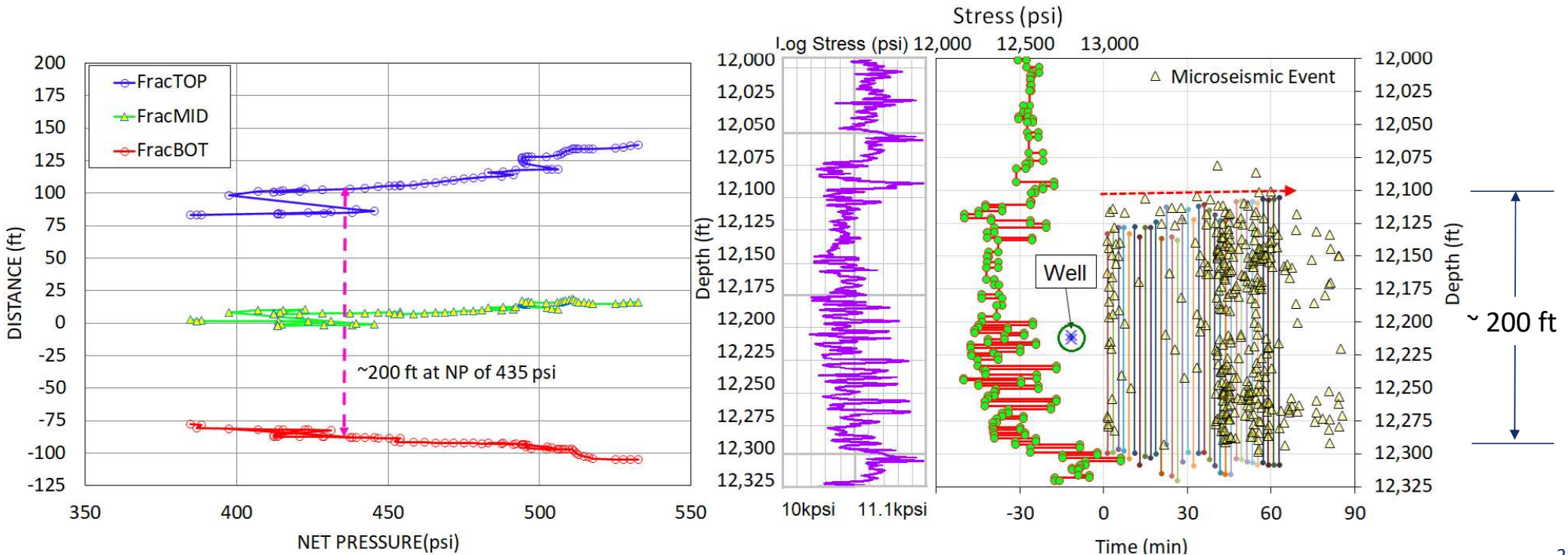


Horizontal Well Case History...



- Case History #5: Contd..

- Fracture location and h_f vs. NP plot generated using velocity based apparent K_{IC} .
- With requisite NP achieved early, fracture growth is instantaneous as seen in MS data.



Summary and Conclusions



- Estimation of fracture height growth is important from both well planning and well performance perspectives.
- Semi-analytical multi-layered model can predict height growth with reasonable accuracy, but for some cases fluid-flow in the fracture cannot be ignored.
- The uncertainty of fracture toughness can be addressed by adopting dynamic velocity-based calculations.
- The fracture location and height versus net pressure mapping provides a reasonable estimate of potential fracture growth that can occur in a treatment.
- Field observations indicate that high initial injection rates result in rapid height-growth whereas low rate/viscosity combination can promote extension.
- Semi-analytical solutions such as presented here can be successfully applied to various reservoir and treatment types.



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